## Physics I Lecture02－Physics \＆ measurements－I

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## CONTENTS

1. Measurement Standard - Length, Mass, and Time
2. Matter \& Physical Model
3.Dimensional Analysis
3. Unit Conversion
4. Estimates and Order of Magnitude
5. Significant Figures

## WHAT IS PHYSICS?



## WHAT

## WHAT IS PHYSICS?

## Classical Mechanics

mechanics (rotation, energy, gravitation), mechanical waves, thermodynamics, electromagnetics atomic physics, nuclear physics, solid state physics


## Quantum Mechanics

## 1. MEASUREMENT STANDARD LENGTH, MASS, AND TIME

The international system (SI) of units:
Length - Meter (m)
Mass - kilogram (kg)
Time - second (s)
The English system of units:
Length - inch (in., 2.54 cm ), foot (ft., 12 inches), mile (mi, 1.609 km )
Mass - pound (lb, 0.454 kg ), ounce (oz, $1 \mathrm{lb}=16 \mathrm{oz}$ )
Time - second (s)
The derived units:
Force - Newton ( $\mathrm{N}, 1 \mathrm{~N}=1 \mathrm{~kg} \mathrm{~m} / \mathrm{s}^{2}$ )
Energy - Joule ( $\mathrm{J}, 1 \mathrm{~J}=1 \mathrm{~kg} \mathrm{~m}^{2} / \mathrm{s}^{2}$ )

## 1. MEASUREMENT STANDARD LENGTH, MASS, AND TIME

The units in electromagnetics:
Unit for electric current: ampere (A)
Charge unit: Coulomb (C, $1 \mathrm{C}=1 \mathrm{~A}$ s)
Voltage unit: $\operatorname{Volt}\left(\mathrm{V}, 1 \mathrm{~V}=1 \mathrm{~J} / \mathrm{C}=1 \mathrm{~kg} \mathrm{~m}^{2} \mathrm{~s}^{-2} / \mathrm{A} \mathrm{s}\right)$


$$
1 \mathrm{~V}=1 \mathrm{~kg} \mathrm{~m}^{2} \mathrm{~s}^{-3} \mathrm{~A}^{-1}
$$

The units in thermodynamics:
Ambiguous unit for temperature: Kelvin (k)
Thermal conductivity: W / m K = kg m / K s²
The units used in Lab:
Pressure: PSI (lb / in.², 1 atm = 14.7 PSI,
$1 \mathrm{~atm} \cong 1 \mathrm{kgw} / \mathrm{cm}^{2}$ )

## 1. MEASUREMENT STANDARD LENGTH, MASS, AND TIME

The standard of length:
~1799 - 1 meter -> one ten millionth of the distance from the equator to the north pole - Earth based standard
~1960 - 1 meter -> distance between two lines on a specific Ptlr alloy bar stored in France
~1970 - 1 meter -> 1650763.73 wavelengths of orange-red light emitted from a Krypton-86 lamp ( 605.78 nm visible light)

~1983 - 1 meter -> the distance traveled by light in vacuum during a time of 1/299 792458 s , where the light is of wavelength

## 1. MEASUREMENT STANDARD LENGTH, MASS, AND TIME <br> $$
I L B=m g
$$

The standard of mass:
since $1887-1 \mathrm{~kg}$-> the mass of a specific Ptlr alloy cylinder, kept at the International Bureau of Weights and Measures at Severes, France

In November 2018, the international scientific community plans to redefine the kilogram, freeing it from its embodiment in one golf-ball-sized artifact, and basing it instead on a constant of nature.- mentioned in NIST report

http://museum.nist.gov


Google map

$$
V=v B L \rightarrow I V=m g v
$$

$$
V=\frac{h f}{2 e}, \frac{1}{R}=N \frac{e^{2}}{h}
$$


https://www.youtube.com/watch?v=0o0jm1PPRuo


Animated Gif image from the report - "Redefining The Kilogram", NIST (http://www.nist.gov)

## 1. MEASUREMENT STANDARD LENGTH, MASS, AND TIME

The standard of time:
before 1967 - mean solar day is the standard of time, a secomd is 1 / 86400 of a mean solar day
after 1967 - after the invention of "atomic clock", one second is 9192631770 times the period of vibration of radiation from the Cs-133 atom

2004 Aug 27, NIST Unveils Chip-Scale Atomic Clock, "cesium vapor confined in a sealed cell and probed with light from an infrared laser"


## 1. MEASUREMENT STANDARD LENGTH, MASS, AND TIME

Prefix:



2016 May, http://physics.nist.gov/cuu/Units/prefixes.html
https://ipkk.com/read/278308.html

## 1. MEASUREMENT STANDARD LENGTH, MASS, AND TIME

## some number with units that YOU MUSt know:

## Length:

Radius of the Earth: $6400 \mathrm{~km}, 6.4 \times 10^{6} \mathrm{~m}$
Altitude of a satellite: 200 km above the Earth surface
Diameter of a hydrogen atom: $10^{-10} \mathrm{~m}, \mathrm{r}=0.529 \AA$
Diameter of a proton: $10^{-15} \mathrm{~m}=1 \mathrm{fm}$
Mass:
Human: $7 \times 10^{1} \mathrm{~kg}$
Hydrogen atom: $1 * 10^{-3} / 6.02 * 10^{23}=1.67 * 10^{-27} \mathrm{~kg}$ Time:

Period of audible sound waves: $10^{-3} \mathrm{~s}$
Period of visible light waves: $10^{-15} \mathrm{~s}$
Magnetic Field:
B on the Earth: 0.5 Gauss


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## 2. MATTER \& PHYSICAL MODEL

Niels Bohr


Dalton: All elements are composed of atoms.

## Thomson: Plum Pudding Model

Rutherford: atoms consisted of a small dense center (named nucleus) filled with positive charges, negatively charged electrons were scattered surrounding the nucleus and were held in orbit.


Bohr: electrons in fixed, circular orbits, more electrons in outer orbits and those in outer orbits have higher energy, there are certain energy transition for electrons from inner (outer) to outer (inner) orbits.
Modern theory: wave description

## 2. MATTER \& PHYSICAL MODEL



## 2. MATTER \& PHYSICAL MODEL

Density ( $\rho=m / V$ ) of Materials:
Example: A solid cube of aluminum has a volume of $0.216 \mathrm{~cm}^{3}$. It is known that 27.0 g of aluminum contains $6.02 * 10^{23}$ atoms. How many atoms are there in the cube?

$$
\begin{aligned}
& m=\rho V=2.7 \times 0.216(\mathrm{~g}) \\
& \quad \frac{0.5832}{27}=0.0216(\mathrm{~mol}) \\
& 0.0216 \times 6.02 \times 10^{23}=1.30032 \times 10^{22} \cong 1.3 \times 10^{22}
\end{aligned}
$$

| Material | Density $\left(\mathrm{g} / \mathrm{cm}^{3}\right)$ |
| :---: | :---: |
| Gold | 19.3 |
| Lead | 11.3 |
| Copper | 8.93 |
| Iron | 7.87 |
| Aluminum | 2.7 |

## 3. DIMENSIONAL ANALYSIS

Example: It is proposed that the radial acceleration $a_{r}$ is proportional to the speed $v$ and the radius $r$ as $a_{r}=k v^{m} r^{n}$, where $n, m$ are two exponents and $k$ is a dimensionless const.
Please use the dimensional analysis to determine the two exponents.

| Quaniity | Symbol | Dimension |
| :---: | :---: | :---: |
| Area | A | $\mathbf{L}^{2}$ |
| Volume | V | $\mathbf{L}^{3}$ |
| Speed | V | $\mathbf{L} / \mathbf{T}$ |
| Acceleration | a | $\mathbf{L} / \mathrm{T}^{2}$ |
| Force | f | $\mathbf{M L} / \mathrm{T}^{2}$ |
| Pressure | D | $\mathbf{M} / \mathrm{LT}^{2}$ |
| Density | d | $\mathbf{M} / \mathbf{L}^{3}$ |
| Energy | E | $\mathbf{M L} \mathbf{L}^{2} / \mathrm{T}^{2}$ |
| Power | $\mathbf{P}$ | $\mathbf{M L} \mathbf{T}^{2} / \mathrm{T}^{3}$ |

$$
\begin{gathered}
v: L^{1} T^{-1} \quad r: L^{1} \quad a_{r}: L^{1} T^{-2} \\
L^{1} T^{-2}=\left(L^{1} T^{-1}\right)^{m}\left(L^{1}\right)^{n} \\
m=2, n=-1
\end{gathered}
$$

## 4. UNIT CONVERSION

Write down all the details - number \& unit for conversion

$$
\begin{gathered}
5 \mathrm{in} .=5 \mathrm{in} . \times\left(\frac{2.54 \mathrm{~cm}}{1 \mathrm{in.}}\right)=12.7 \mathrm{~cm} \\
161 \mathrm{~km}=161 \mathrm{~km} \times\left(\frac{1 \mathrm{mi}}{1.61 \mathrm{~km}}\right)=100 \mathrm{mi}
\end{gathered}
$$

Example: The $1^{\text {st }}$ car is moving with a speed of $42 \mathrm{~m} / \mathrm{s}$ and the $2^{\text {nd }}$ car is moving with a speed of $55 \mathrm{mi} / \mathrm{h}$. Are the drivers exceeding the speed limit of $100 \mathrm{~km} / \mathrm{h}$ ?

$$
\begin{aligned}
& \text { 1st Car: } \frac{42 \mathrm{~m}}{s}=\frac{42 \mathrm{~m}}{s} \times \frac{1 \mathrm{~km}}{1000 \mathrm{~m}} \times \frac{3600 \mathrm{~s}}{1 \mathrm{~h}}=151.2 \mathrm{~km} / \mathrm{h} \\
& \text { 2nd Car: } \frac{55 \mathrm{mi}}{\mathrm{~h}}=\frac{55 \mathrm{mi}}{\mathrm{~h}} \times \frac{1.61 \mathrm{~km}}{1 \mathrm{mi}}=88.55 \mathrm{~km} / \mathrm{h}
\end{aligned}
$$

## 5. ESTIMATES AND ORDER OF MAGNITUDE

Scientific notation, two or three digits with the multiplier of
the power of $10-N_{1} \cdot N_{2} N_{3} \times 10^{N_{4}}$
Order of magnitude without the prefix of digital number
change $N_{1} \cdot N_{2} N_{3}$ to $10^{N_{5}}$

$$
\begin{aligned}
& N_{1} \cdot N_{2} N_{3}>10^{0.5} \rightarrow 10^{1} \\
& N_{1} \cdot N_{2} N_{3}<10^{0.5} \rightarrow 10^{0}
\end{aligned} \quad 10^{0.5}=\sqrt{10}=3.162
$$

Example: There are $N_{A}$ atoms in 12 g of carbon. If counting 1 atom takes 1 s , how long does it take to count all atoms in 1 g of carbon?

$$
1 g \times \frac{6.02 \times 10^{23}}{12 g} \div\left(\frac{1 g}{1 s}\right) \times\left(\frac{1 D}{86400 s}\right) \times\left(\frac{1 Y}{365 D}\right) \cong 1.6 \times 10^{15}
$$

## 6. SIGNIFICANT FIGURES

Measurements: precise digits with the first estimated digit.


How to count the significant figure?
The rule of addition \& subtraction: no significant figures beyond the last decimal place where both of the original numbers have significant figures.

$$
\begin{gathered}
1.002+11.0=12.0 \\
10.25-1.1=9.15 \cong 9.2
\end{gathered}
$$

The rule of multiplication \& division: no greater than the least number of significant figures in any of the numbers. $\quad 2.12 \times 3.214=6.81368 \cong 6.81$

## 6. SIGNIFICANT FIGURES

The standard deviation shall be less than the lowest decimal number.

$$
3.21 \pm 0.04 \quad 3.21 \pm 0.05
$$

Example: A rectangle has a length of $6.21 \pm 0.02 \mathrm{~m}$ and a width of $7.8 \pm 0.2$ m . Please calculate the area.

$$
\begin{aligned}
& (6.21 \pm 0.02) \times(7.8 \pm 0.2)=48.438 \pm 0.156 \pm 1.242 \\
& =48.438 \pm 1.398=48 \pm 1
\end{aligned}
$$

## ACKNOWLEDGEMENT



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自主愛學習計畫


